

# Waddington's Revision Of Haldane

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I have repeatedly objected to Waddington's revision of Haldane's basic population genetics equations being ignored within gene centric Neo Darwinism. Jim Menegay expressed interest in Waddington's revision and asked the professionals that post here for clarification. None has been forthcoming. Therefore I have decided to post some of the photostate that I have. The cover sheet was lost so I cannot give the exact reference. As I recall they were copied from Waddington's book "The Evolution Of An Evolutionist". Perhaps somebody else can supply the exact reference. Here are what I consider to be the appropriate parts which I will post without comment.

----- Beginning of Waddington's Revision of Haldane -----

## THE NECESSITY TO CONSIDER MORE THAN ONE ENVIRONMENT

The strict Neo-Darwinist paradigm is unsatisfactory in another respect, namely, that it involves only one uniform environment, through which natural selection is exerted in a form which requires specification by one single coefficient for each type of biological entity. Again, as with the omission of the phenotype, there are several different objections to this – though, perhaps they should be regarded as different aspects of a basic general objection.

To put the matter abstractly first: there are only two sources of evolutionary change; alterations in the environment, or alterations in genes. A paradigm in terms of a single uniform environment implies either attainment of an equilibrium, or evolutionary changes brought about by the appearance of new genes. But the latter is a very weak prop to rely on, since it is normally held that all possible

mutations are constantly occurring at definite frequencies. One could perhaps escape this dilemma by appealing to rare mutational events involving large scale restructuring of the geno-type (additions, deletions, inversions, etc.), or rare incorporation of large masses of genetic information by processes such as introgressive hybridization, incorporation of episomes etc, but this would be an uncomfortable basis for a general theory of evolution.

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 On a more pragmatic level, one may ask whether the concept of a single uniform environment is ever even conceivably applicable in the real world, which appears inescapably heterogeneous. And if it is not, it should be remembered that evolution provides mechanisms by which any initial inhomogeneity will become either exaggerated in kind or increased in the number of sub-regimes. For instance, if we start with a total universe containing two environmental regimes (niches) A and B, each dominated by a biological species A' or B', that it will always be possible for some evolutionary descendant of one or other of these species to delimit as its own niche some appropriate function of the previously existing entities F(A,B,A'B'); indeed there is an infinite set of such functions to be used in this way. This is the general explanation for one of the features of evolution which seems to prove most puzzling to physical scientists, who ask why such an enormous variety of different types should have been produced, although the existence of primitive organisms such as bacteria, at the present day, proves that they are functionally quite 'fit' enough to survive.

[..]  
 Suppose there are two clones A and a, and two environments X and Y, with frequencies p and 1-p. As case 1 let us assume that a proportion q of organisms is selected in X and 1-q in Y. Then for each clone we have:

Developed in X	Developed in X	Developed in Y	Developed in Y
Selected in X	Selected in Y	Selected in X	Selected in Y
pq	p(1-q)	q(1-p)	(1-p)(1-q)

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Suppose clone a has perfect adaptiveness, i.e. always has full natural selective efficiency in the environment in which it developed. Then its coefficients would be :

$$\frac{1 - k_1}{1 - k_2}$$

But let clone a be fully canalized for X, i.e. show full natural selective efficiency in X whatever environment it had developed in. Its coefficients would be:

$$\frac{1 - k_3}{1 - k_4}$$

Simplifying further, we may assume that the chance of being selected within an environment is proportional to the frequency of that environment, i.e.  $q=p$ . Further, let us take  $k_1=k_2=k$  and  $k_3=k_4=k'$ . Then the freq of A and a in generation n were  $1-u$  and  $u$ , respectively, in generation n+1 they will be:

[JE:- I will use the # to denote the sub case]

$$\begin{aligned} A_{\#}(n+1) &= (1-u) [p^2 + (1-p)^2 + 2p(1-p)(1-k)] \\ &= (1-u) [1 - 2p(1-p)k] \\ a_{\#}(n+1) &= u[p^2 + p(1-p) + (p(1-p) + (1-p)^2)k'] \\ &= u[1 - (1-p)k'] \end{aligned}$$

Therefore:

$$u_{\#}(n+1) = \frac{u[1 - (1-p)k']}{u[1 - (1-p)k'] + (1-u)[1 - 2p(1-p)k]}$$

change in  $u = u_{\#}(n+1) - u_{\#}(n)$  is positive if

$$u[1 - (1-p)k'] - u^2[1 - (1-p)k'] - u(1-u)[1 - 2p(1-p)k]$$

is positive, i.e. if

$$1 - (1-p)k' > 1 - 2p(1-p)k$$

$$k' > 2pk$$

Thus, as might be expected, which clone is favoured depends not only on the selection coefficients but on the freq' of the environments, and the larger the freq' of environment X the more likely it will pay to canalize for it.

Mendelian Recessive in a diploid

This is the classical paradigm case. In the Neo Darwinist formulation, one assumes a fully recessive gene 'a' in freq 'u'. Then the array of zygotes

in generation n is  $(1-u)^2 AA$ ,  $2u(1-u)Aa$ , and  $u^2 aa$ . In generation n-1 this will be changed to  $(1-u)^2 AA$ ,  $2u(1-u) Aa$ ,  $u^2(1-k)aa$ .

In the post-Neo-Darwinist scheme, we have to envisage two environments X and Y in freq' p and  $1-p$ . We can make the same simplifying assumption

that both development and selection occur in these environments in proportion to their freq. We have to assign selection coefficients to the phenotypes derived from all three genotypes in the different combinations of development and selection. These would be as follows for a case in which the dominant gene produces a fully adaptive development, while the recessive produced canalization for environment X.

Dev' in X Dev' in X Dev' in Y Dev in Y  
 Sel' in X Sel' in Y Sel' in X Sel' in X

freq'

AA  $(1-u)^2$   $1-k$   $1-k$   $1$   
 Aa  $2u(1-u)$   $1-k$   $1-k$   $1$   
 aa  $u^2$   $1-k'$   $1-k'$   $1$

It is easy to show that the zygotic freq' in the next generation will be:

AA  $(1-u)^2 [1-2pk(1-p)]$   
 Aa  $2u(1-u) [1-2pk(1-p)]$   
 aa  $u^2 [1-k'(1-p)]$

Whence

$$u \#(n+1) - u \#(n) = \frac{u^2(1-u)[1-k'(1-p)] - [1-2pk(1-p)]}{(1-u)^2[1-2pk(1-p)] + u^2[1-k'(1-p)]}$$

This is positive if  $k'$  is less than  $pk$ .

Alternatively, one may consider the situation in which AA and Aa are canalized for environment X, while aa produces an adaptive phenotype. The selection coefficients will be:

Dev' in X Dev' in X Dev' in Y Dev in Y  
 Sel' in X Sel' in Y Sel' in X Sel'  
 in X

AA and aa  $1-k$   $1-k$

aa  $1-k'$   $1-k'$   
 $1$

>>From this it turns out that  $u \#(n+1) - u \#(n)$  is positive if  $2pk'$  is less than  $k$ . Thus if environment X is the more frequent one ( $p$  greater than 0.5), a gene producing canalization (case 1) can make its way against an adaptive gene in the face of a less favourable ratio of selection coefficients than can an adaptive recessive competing

with a canalization dominant.

Conclusions

[..]

What I wished to do was to exhibit a scheme of basic ideas which directs attention towards, rather than away from, the problems which are of most importance for evolutionary theory at the present time. By far the greatest advance in our knowledge of evolution which has occurred in recent years has been the discovery of the enormous range and variety of genetic variation which is present in natural populations. It seems certain that one of the important determinants of this situation is the fact that such populations exist in heterogeneous environments, so that the applied selection criteria are not the same for all individuals.

[...]

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I apologize in advance for any errors in the copying of this material. I am happy to go back and check anything that is incorrect. My scanner cannot scan mathematics so it all had to be done by hand.

I sincerely hope that this posting stimulates discussion in what I consider to be one of the most important subjects in evolutionary theory: the relationship between model and theory. I hope that Felsenstein will put to one side the differences between us and honour Waddington by participating in this discussion of one of Waddington's most important contributions.

Regards,

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## Waddington's Revision Of Haldane

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