

Re: Existence, Self-identity and Uniqueness.

Source: <http://sci.tech-archive.net/Archive/sci.logic/2006-12/msg00493.html>

- *From:* William Elliot <marsh@xxxxxxxxxxxxxxxxxxxxx>
 - *Date:* Thu, 28 Dec 2006 22:01:53 -0800
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On Thu, 28 Dec 2006, Jan Burse wrote:

William Elliot wrote:

On Thu, 28 Dec 2006, Jan Burse wrote:
 We agree that it's theorem when $(\exists!x)F(x)$.
 In the event $\sim(\exists!x)F(x)$, the premise
 $\exists xF(x) = y$
 is false, thus promoting again the whole statement to truthood.

Ok, thanks.

What's the theorem that's part of this comment?
Please don't over clip, it derails continuity of thought.

Yes, the " $x=y \rightarrow (A0(x) \leftrightarrow A0(y))$ " is not the counter example. But the "forall x A0(x)" is the counter example.

forall x A0(x) is true, but A0(the x:F0x) is false. That violates the following valid inference in FOL=:

$$\begin{array}{l} G \vdash \text{forall } x \text{ } A0(x) \\ \hline G \vdash A0(t) \end{array}$$

Derived rules of inference, bah.

The axiom

$(\forall x)G(x) \rightarrow G(t)$

for any term t, you claim, cannot be used willy nilly with $\exists xF(x)$.

Case $(\forall x)F(x)$

case $(\forall x,y) x = y$

$(\forall x)G(x) \rightarrow G(\exists xF(x))$

Re: Existence, Self-identity and Uniqueness.

case $(\exists x, y) x \neq y$
 $\sim G(\exists x F(x))$
 $\sim[(\forall x)G(x) \rightarrow G(\exists x F(x))]$
Case $\sim(\forall x)F(x)$
 $(\forall x)F(x) \rightarrow G(\exists x F(x))$

That is true, the axiom is for terms of the language,
not for syntactic term constructs, synthetic terms.

Moral of the story: don't use $\exists x F(x)$ without $(\exists! x)F(x)$.