

Re: Cantor's definition of set

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 - *Date:* Sat, 27 Oct 2007 00:15:14 +0200
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On Fri, 26 Oct 2007 14:45:48 -0700, John Jones <jonescardiff@xxxxxxx> wrote:

'2' is a numeral. 2 is a number.

Please try to get that straight before engaging in even more idiotic babble, ok?

"2" is a name we use to denote the number 2.

Of course, there are other names too, "1 + 1" for example. Indeed,

$1 + 1 = 2$.

(See!)

Now you claim:

The number 2 is always generated by an application, so I cannot propose simply 2. I cannot say 2 is a number and leave it at that. I must specify, and not simply assume, an application that generates it.

Let's -for the sake of the argument- accept that point of view.

YES, We DO specify the number 2 in math. (And especially set theory).

Ever heard of the so called Peano axioms? There we take (exactly) ONE natural number, namely 0, for granted.

Axiom: 0 is a natural number.

Then we can define the number 1 as successor of 0:

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$1 =_{df} s(0)$,

and the number 2 as successor of 1:

$2 =_{df} s(1)$.

Hence:

$2 = s(s(0))$.

(With other words, the number 2 is the successor of the successor of 0. This is the specification you asked for.)

Now in axiomatic set theory we do not even take the number 0 "for granted". But we define it the following way:

$0 =_{df} \{ \}$,

where $\{ \}$ denotes the so called empty set. And we can **PROVE** in axiomatic set theory that there is an (actually exactly one) empty set.

Even if numbers existed in a third Platonic realm as stand-alone real entities, I would not be able to recognize them as numbers except by employing an application, like counting.

Let's –for the sake of the argument– accept that poin