

Re: Largest Set in ZFC?

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<SNIP>

> The definition is:

> $\{S\} = \{S S\}$

> and, of course $\{S S\}$ we get from pairing..

Thanks. I was curious how that worked.

If S is a set then pairing says $\{S,S\}$ is a set
and extensionality says $\{S,S\} = \{S\}$.

*** I had never even noticed the issue, interesting.

It seems AoI is deliberately vague about what
sets are members of X . Why is that?

I don't know the motivation of the actual people who wrote it, but the
reason I personally would give is this: We don't NEED to be any more
specific, since separation does the rest of the job for us to get to
the specific set w that we want.

*** I know much less about this topic than you do, but it seems there is a more fundamental reason for the
vagueness of the definition of X . If anybody could produce a specific such X , then they would have a model
of ZF (a collection of sets that satisfy ZF). This would prove the consistency of ZF. AFAIK, there is no
theoretical reason why such a set X could not be described, but none ever has, and it seems pretty obvious
that none ever will. Hence the requirement to vague it up a bit.