

Re: Transforming expressions into ellipse normal form

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In article <s2dv31lhdkdlvik7jmuvtqoe4laom1mdmk@4ax.com>,

Roboy B <markieboy03@gmail.com> writes:

>How to transform the expression $[3x^2-2xy+3y^2]$ by trigonometric

>method with coordinate transformation and matrix diagonalization

>method?

this is $\begin{bmatrix} x & y \end{bmatrix} \begin{bmatrix} 3 & -1 \\ -1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$

now compute the two eigenvalues of the 2 by 2 matrix with eigenvectors normalized to euclidean length 1. Say

$$U^*A*U = \text{diag}(\lambda_1, \lambda_2)$$

then

$$A = U * \text{diag}(\lambda_1, \lambda_2) * U'$$

insert this above set $\begin{bmatrix} v, w \end{bmatrix} = U^* \begin{bmatrix} x, y \end{bmatrix}'$, done . (' is transposition)

hth

peter