

Re: A functional measure of roughness

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The measure of roughness based on the Bezier
which is like a Lyapunov exponent average, but more sensitive:

It turns out to be like a second derivative:

Measure[n]=Sum[Log[1+Abs[f'(x(i))]/4],{i,1,n}]/n

Limit[Measure[n],n->Infinity]=rho

The roughness measure is related to the Lyapunov exponent average by

$k = \frac{\text{Sum}[\text{Log}[f'(x(i))], \{i, 1, n\}]/n}{\text{Sum}[\text{Log}[1 + \text{Abs}[f'(x(i))]/4], \{i, 1, n\}]/n}$

k is close to 2 for the primes.

So I have actually found two measures.

Roger Bagula wrote:

- > *In thinking of a way to get a better than Lyapunov, Hausdorff or Kolmogorov*
- > *measure of dimension, I thought of this:*
- > *F(curve)=0 if smooth and continuous*
- > *F(curve)<>0 if rough or discontinuous*
- > *The best measure of dimensional roughness (Mandelbrot's way of*
- > *expressing it) is the*
- > *Lyapunov exponent (or maybe the Hurst exponent?).*
- > *Box counting or capacity/entropy dimension of the Kolmogorov type*
- > *is too big most of the time*
- > *while Hausdorff being very cut-off measure like*
- > *is usually too small.*
- > *The trouble with Lyapunov is that it depends on a derivative*
- > *and unless you are talking about a fractional derivative,*
- > *many fractal functions are of the Weierstrass fractal type*
- > *where the classical derivative doesn't exist.*
- >
- > *I did some work on Bezier functions in IFS in the past*
- > *and fractional partial derivatives of an angular sort as well.*
- > *I came to realize that the three point Bezier function of an iterative*
- > *sequence in n:*
- > $\text{Bezier}[p,n] = p^2 * f(n+2) + 2 * p * (1-p) * f(n+1) + (1-p)^2 * f(n)$
- > *is such that if smooth and continuous:*
- > $f(n+1) = \text{Bezier}[1/2,n] = f(n+2)/4 + f(n+1)/2 + f(n)/4$
- > *So that the function:*
- > $\text{delta}[n] = f(n+2)/4 + f(n+1)/2 + f(n)/4 - f(n+1)$
- > *is a measure of the roughness.*
- > *Putting this measure in an Lyapunov average type function:*

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- > $Measure[n]=Sum[Log[1+delta[i]],\{i,1,n\}]/n$
- > *I tried this out by comparing it to a known rough set, the primes*
- > *and it's Lyapunov integer difference average.*
- > *In this experiment the new Bezier roughness measure performs better than the*
- > *Lyapunov equivalent over the same range in detecting roughness.*
- > *Respectfully, Roger L. Bagula*
- >
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