

Re: A qn on primitive recursive functions

Source: <http://sci.tech-archive.net/Archive/sci.math/2004-09/0088.html>

From: peter_douglass (*baisly_at_gis.net*)

Date: 08/31/04

Date: Tue, 31 Aug 2004 13:17:30 GMT

"peter_douglass" <baisly@gis.net> wrote in message
news:1L_Yc.99200\$mD.71079@attbi_s02...

> *"Peter Smith" <ps218@cam.ac.uk> wrote in message*

> *news:ps218-5624F5.09593031082004@pegasus.csx.cam.ac.uk...*

>

> > *The following is true:*

>

> > *There is no effective way of deciding, of some arbitrary primitive*

> > *recursive function $f(x)$, whether there are values x such that*

> > *$f(x) = 0$.*

>

> > *You can prove that readily if you already know about Turing machines and*

> > *halting problems, or already know that the total recursive functions are*

> > *not effectively enumerable [for if we can effectively tell which p.r.*

> > *functions are regular, we could effectively enumerate the total*

> > *recursive function, because we could tell which recipes for functions*

> > *involved regular minization].*

> > *But how about a more direct proof that doesn't go via results about*

> > *Turing machines or recursive functions?*

Addendum: If you aren't interested in machines per se, but just
primitive recursive functions, replace "machine" everywhere in the
proof by "partial function". i.e. M is a set of partial functions,
 m is an element of that set etc.

--PeterD