

Re: induction vs Cantor

Source: <http://sci.tech-archive.net/Archive/sci.math/2004-12/2480.html>

From: Poker Joker (*Poker_at_wi.rr.com*)

Date: 11/28/04

Date: Sun, 28 Nov 2004 18:52:02 GMT

"J.E." <troubled6man@yahoo.com> wrote in message
news:39d6e584.0411271230.3f762cf3@posting.google.com...

<snipped>

> If you take the union of all the L_n , then you get a countable set, so
> you can construct a NEW list $L_{\{\omega\}}$ that lists every element in L_1
> and all the D_n . But if you apply the diagonal argument to $L_{\{\omega\}}$
> then you get $D_{\{\omega\}}$ which isn't in the union, so it isn't in L_1 or
> any of the D_n . If you made a new list $L_{\{\omega+1\}}$ which had
> $D_{\{\omega\}}$ in it, then I could use the diagonal argument again to get
> $D_{\{\omega+1\}}$. The whole point is that for any list L_X , there is a
> real D_X that isn't on L_X . So you can make as many L 's as you want,
> but there is always another D . It's like the proof of an infinite
> number of primes. One way to do it is to assume that there are a
> finite number p_1 to p_n then multiple them together and add one. This
> new number is not divisible by any of the others, and so it's a new
> prime. The diagonal argument takes a countable number of things and
> produces "another one" not matter how many "countable" things there
> were.

Yes, its like the primes. There are only countably many primes.

>> > Have you followed through with your process a little
>> > bit with a particular L_0 ? All of the D_n 's have the
>> > property that, if $k > n$, then the first $(n/2)-1$ digits
>> > of D_n match the first $(n/2)-1$ digits of D_k .
>>
>> No I haven't but I would have to add that there are
>> countably many ways of creating "anti-diagonal" numbers
>> so I'm not certain how you are doing that analysis.
>
> The thing is that there are as many ways to make anti-diagonal numbers
> as there are lists, because for every list there is another "new"
> antidiagonal number. So as in my example above if you union L_n
> together to get a "new" list (which we'll call $L_{\{\omega\}}$), then there
> is a "new" anti-diagonal.

sci.math: Re: induction vs Cantor

All the descriptions of the methods for creating a number not in the list forms a countable set. You can call one of the lists "new" but it's just one list. We always have room for one more in our countable set.