

Cantor and the binary tree

Source: <http://sci.tech-archive.net/Archive/sci.math/2005-05/msg04384.html>

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 - *Date:* 24 May 2005 05:58:22 -0700
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Cantor and the binary tree.

If we accept that, in binary digits, $\text{SUM}\{n = 1 \dots \infty\} 2^{-n} = 0.111\dots = 1$

then all the real numbers of the interval $[0,1]$ are realized as infinite paths of the binary tree

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0 1
0 1 0 1
.....

too (read from top to bottom). Each number is given by a path stretching over infinitely many nodes (bits). All nodes (bits) of the tree are countable. The paths are not, according to Cantor's famous diagonal proof.

But we find that, up to line number n , there are $-1 + 2^{(n+1)}$ nodes whereas 2^n different paths arrive at and $2^{(n+1)}$ different paths spring off from line number n . Hence, in the enumerated domain, there is at most one more path than nodes. After leaving any finite line number n (if it is reasonable to make such a distinction) we can no longer apply these formulae. But we know that any new branching increases the number of paths by 1 and, by definition, the number of nodes by 1 too (because any branching is a node). Therefore, the number of paths always equals that of the nodes + 1. It is simply impossible to assume that one of these numbers becomes uncountably infinite while the other remains countably infinite.

Regards, WM

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- *Follow-Ups:*
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 - ◇ *From:* Gottfried Helms

Cantor and the binary tree

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- ◆ **Re: Cantor and the binary tree**
 - ◇ From: Robert Kolker
- ◆ **Re: Cantor and the binary tree**
 - ◇ From: David C . Ullrich
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