

Re: conditional probability

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Tino wrote:

"Stephen J. Herschkorn" <sjherschko@xxxxxxxxxxxxx> wrote in message
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Tino wrote:

<>If the only information I know is that $P(A)$, $P(B)$, $P(C)$, $P(A \text{ and } B)$, $P(A \text{ and } C)$ and $P(B \text{ and } C)$, (A , B and C are not independent) is there a way to compute $P(A \text{ and } B \text{ and } C)$?

No. You need seven parameters to specify the probabilities of all the atoms (i.e., there are seven degrees of freedom), yet you give only six parameters above. You should be able to determine bounds on $P(ABC)$.

Some pointers on how to generate an upper bound would be useful.

With binary indices, let p_{ijk} denote the probabilities of the atoms.

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I.e., letting ' denote complement, $p_{111} = P(ABC)$, $p_{110} = P(ABC')$, $p_{101} = P(AB'C)$, etc. You have seven linear equations in eight variables; here are three of them:

$$\begin{aligned} \text{sum}(j,k; p_{1jk}) &= P(A) \\ \text{sum}(k; p_{11k}) &= P(AB) \\ \text{sum}(i,j,k; p_{ijk}) &= 1. \end{aligned}$$

Solve for all the other p_{ijk} 's in terms of p_{111} . Each of these values must be between 0 and 1, inclusive. This gives you seven inequalities that p_{111} must satisfy.

Numerically, you can also do this by linear programming.

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