

# Re: Rational and irrational numbers

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*Source:* <http://sci.tech--archive.net/Archive/sci.math/2005-08/msg05729.html>

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- *From:* [klewis@xxxxxxxxxxxxxxxxxx](mailto:klewis@xxxxxxxxxxxxxxxxxx) (Keith A. Lewis)
  - *Date:* Mon, 29 Aug 2005 17:20:10 +0000 (UTC)
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deepkdeb@xxxxxxxx writes in article <1125252423.614978.59470@xx> dated 28 Aug 2005 11:07:03 -0700:

>Correction and modification:

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>Given situations:

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> $\sqrt{a} + \sqrt{b} = u^k$  (1);  $\sqrt{a} - \sqrt{b} = v^k$  (2)

> $uv$  is an integer, odd  $k > 5$ , both  $a$  and  $b$  are nonsquare integers  $> 0$ .

>

>Assertion:  $u$  and  $v$  must be of the form (3) and (4) where

> $u = A\sqrt{g} + B\sqrt{h}$  (3);  $v = A\sqrt{g} - B\sqrt{h}$  (4)

> $g, h$  are nonsquare integers and  $A, B$  are integers  $> 0$ .

Still incorrect. I am not going to provide a specific counterexample (although I believe  $(\pi, 1/\pi)$  suggested by another poster still stands), just an argument based on cardinality.

The set of ordered pairs  $(x,y)$  s.t.  $xy=z$  has the cardinality of  $\mathbb{R}$ . Remove the rational points and it's still  $|\mathbb{R}|$ .

Your expression of  $x$  and  $y$  as functions of a finite number of (now 4) integers has the cardinality of  $\mathbb{N}^4$  which is equal to that of  $\mathbb{N}$ . There must be some solutions missing.

--Keith Lewis [klewis@mitre.org](mailto:klewis@mitre.org)

The above may not (yet) represent the opinions of my employer.

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• *Follow-Ups:*

- ◆ [\*\*Re: Rational and irrational numbers\*\*](#)

◇ *From:* quasi

• *References:*

- ◆ [\*\*Rational and irrational numbers\*\*](#)

◇ *From:* deepkdeb

- ◆ [\*\*Re: Rational and irrational numbers\*\*](#)

◇ *From:* deepkdeb

Re: Rational and irrational numbers

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