

Re: How to solve $(2x + 3y)^3$?

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 - *Date:* Thu, 29 Sep 2005 09:23:46 +0100
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dwwdkddb wrote:

I think you're neglecting the number of operations involved in computing the binomial coefficients to make this argument. You have $3C_0$, $3C_1$, $3C_2$ and $3C_3$ to compute, (quite a few multiplications and divisions there) as well as the various powers of 2 and 3 to multiply together.

Like I said, the binomial coefficients

can be most easily had from Pascal's triangle (just involves a few additions). You're probably right about the powers of 2 and 3, but I guess anyone reasonably well-versed in arithmetic knows the first few by heart. (I for one know them up until 2^{10} and 3^5 .)

Sure: knowing the answer in advance always makes it easier :-)

But now you're asking somebody to learn the binomial theorem, and know a relationship between the binomial coefficients and Pascal's triangle, all of which saves maybe a couple of multiplications at the expense of obfuscating what they're actually doing. And even with all that, I doubt whether I'd be significantly faster to work out $(2x+3y)^3$ with the binomial theorem than by just multiplying out.

For a cubic, it's a sledge-hammer to crack a nut. That's not to say that the sledge-hammer doesn't have its uses, and once you have the sledge-hammer and have practised a lot

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with it you can use it for a nut-cracker.

But I'm willing to concede that just which tool is the best for the job depends on the person using it as well as how much they practise with it, so I'll stop niggling away at this now.

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