

# Re: infinity

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Daryl McCullough said:

> Tony Orlow says...

>

>>> A sequence of length  $\aleph_0$  has a domain equal to the set of all

>>> ordinals less than  $\aleph_0$ .

>> So, you are placing  $\aleph_0$  directly after the largest finite?

>

> How many times do you have to be told: There *\*is\** no largest

> finite!  $\aleph_0$  is placed after *\*all\** finite ordinals.

And has no predecessor. Good way to kludge away the largest finite.

>

> Here's a way to visualize countable ordinals that might

> make sense to you.

>

> Take the real number line, and label the point 0 with the

> ordinal 0. Label the point  $1/2$  with the ordinal 1. Label

> the point  $2/3$  with the ordinal 2. In general, label the

> point  $n/(n+1)$  with the ordinal  $n$ . Finally, label the

> point 1 with the ordinal  $\aleph_0$ .

The point 1 is not included unless you allow infinite  $n$ , right?

>

> Note: the finite ordinals are the labels for reals of

> the form  $n/(n+1)$ . There is no largest real of that form,

> but the real 1 is larger than *\*any\** of them.

When  $n=\infty$ .

>

>>> That's what it seems like. Each of those sets you mention

>> has a largest element 1 less than its size.

>

> Right. That pattern holds for every finite set. That's

> because finite sets of naturals have a largest element.

> Infinite sets of naturals *\*don't\** have a largest element.

But then, the largest of tha