

Re: probability of real factorization.

Source: <http://sci.tech-archive.net/Archive/sci.math/2005-12/msg00064.html>

- *From:* "david petry" <david_lawrence_petry@xxxxxxxxxx>
 - *Date:* 30 Nov 2005 15:53:14 -0800
-

Robert Israel wrote:

> In article <1133353263.758335.202840@xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx>,
> <pauldepstein@xxxxxxx> wrote:
>> Let n be a fixed positive integer.
>>
>> Let N also be a positive integer.
>>
>> Randomly select a real monic polynomial in $Z[x]$ of degree n such that
>> all coefficients have absolute value less than N . (Select such that
>> all eligible polynomials have equal probability of being chosen.)
>>
>> As N tends to infinity, what is the limit of the probability, p_n ,
>> that the selected polynomial factors completely over the reals.
>>
>> For $n = 2$, $p_n = 1$ I think.
>
> For $n = 3$, the discriminant of $x^3 + a x^2 + b x + c$ is
> $D(a,b,c) = -27 c^2 + 18 a b c + a^2 b^2 - 4 a^3 c - 4 b^3$.
> The cubic has three real roots iff $D(a,b,c) \geq 0$.
> Note that if $|a|, |b|, |c| \leq N$,
> $D(a,b,c) = a^2 (b^2 - 4 a c) + O(N^3)$
> so as $N \rightarrow \infty$, the probability of three real roots should
> approach the probability that $b^2 - 4 a c > 0$, which is
> $41/72 + \ln(2)/12$ (see Rob Johnson's posting).

I'm posting without doing much thinking here, but...

It looks like the answer for arbitrary degree n might be
 $(41/72 + \ln(2)/12)^{\lfloor n/2 \rfloor}$ where $\lfloor n/2 \rfloor$ is the integer part of $n/2$.

.

-
- *Follow-Ups:*
 - ◆ ***Re: probability of real factorization.***
 - ◇ *From:* Robert Israel

Re: probability of real factorization.

- **References:**

- ◆ **Re: probability of real factorization.**

- ◆ *From:* Robert Israel

- Prev by Date: **Re: Negative Mathematics**

- Next by Date: **Re: equilateral triangles**

- Previous by thread: **Re: probability of real factorization.**

- Next by thread: **Re: probability of real factorization.**

- Index(es):

- ◆ **Date**

- ◆ **Thread**