

Re: bound on eigenvalues...

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- *From:* Robert Low <mtx014@xxxxxxxxxxxxxxxxx>
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comtech wrote:

Robert Low wrote:

José Carlos Santos wrote:

The eigenvalues are the roots of the characteristic polynomial, which is $P(x) = -x^3 + a x^2 + b x + c$, with $a = 0.501$, $b = -0.024089$, and $c = 0.0000524046$. Since it's a third degree polynomial, it can't have more than three roots. Now, since $P(0) = 0.0000524046$, $P(0.05) = -0.0000245449$, $P(0.1) = 0.00165351$, $P(0.4) = 0.00657681$, and $P(0.5) = -0.0117421$, there must be a root between 0 and 0.1, a second one between 0.1 and 0.4, and a third one between 0.4 and 0.5. This proves that all roots are smaller than 0.5.

But I think he **meant** to write that there must be a root between 0 and 0.05, a second one between 0.05 and 0.1, and a third one between 0.4 and 0.5, since that's how the sign changes go.

But these approaches look like numerical... it is perfectly OK for practice ... but here we need analytical methods...

No. Once you know that that a function is continuous on $[a,b]$ and takes on opposite signs at a and b , the intermediate value theorem tells you that it is zero at some point between a and b . You can use estimates of the value of the function (with known errors) to guarantee the sign change.

It's all analysis, but some of it involves numbers.

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