

# Re: Normal families, complex analysis question

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*Source:* <http://sci.tech-archive.net/Archive/sci.math/2005-12/msg04148.html>

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- *From:* "James" <James545@xxxxxxxxxx>
  - *Date:* Thu, 22 Dec 2005 11:11:41 -0500
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"David C. Ullrich" <ullrich@xxxxxxxxxxxxxxxxxx> wrote in message  
[news:ahilq1phdftgt4s1n1cbebtfg3dn0hhorv@xxxxxxxxxx](mailto:news:ahilq1phdftgt4s1n1cbebtfg3dn0hhorv@xxxxxxxxxx)  
> On Thu, 22 Dec 2005 10:20:16 -0500, "James" <James545@xxxxxxxxxx>  
> wrote:

>  
>>Let  $H$  be the family of functions  $h$  analytic on  $D = \{ |z| < 1 \}$  so that  
>>  
>> $h(D)$  is contained in  $C - [-\infty, 0]$ .  
>>  
>>I am trying to show that  $H$  is a normal family.  
>>  
>>So the image of  $h$  is contained in a domain that can be used as a branch of  
>> $\log$ . The function  
>>  
>> $f(z) = [\sqrt{z} - 1] / [\sqrt{z} + 1]$   
>>  
>>maps  $C - [-\infty, 0]$  analytically isomorphically to  $D$ .  
>>  
>>So I have that  $|f \circ h| \leq 1$   
>>  
>>for all  $h$  in  $H$ . I want to show that  $H$  is locally bounded.  
>>  
>>But that is all I can get, and it doesn't help me at all. Any thoughts?  
>  
> You actually have that  $|f \circ h| < 1$  in  $D$ , and this shows  
> that if  $K$  is a compact subset of  $D$  then there exists  $c < 1$   
> such that  $|f \circ h| \leq c$  in  $K$ .

Yes

> That shows that  $h|_K$  takes  
> values in some compact subset of  $C - [-\infty, 0]$ .  
>

Yes, but that is only for this  $h$ .  $c$  depends on  $h$ , and the  $c$  could get arbitrarily close to 1. I agree that for a particular  $h$ , there is a  $c$  like you said, and  $h|_K$  is bounded. But how do you say this uniformly for all  $h$  in  $H$ ?

Re: Normal families, complex analysis question

>>James

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> David C. Ullrich

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• *Follow-Ups:*

◆ *Re: Normal families, complex analysis question*

◇ *From:* David C . Ullrich

• *References:*

◆ *Normal families, complex analysis question*

◇ *From:* James

◆ *Re: Normal families, complex analysis question*

◇ *From:* David C . Ullrich

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