

# Re: JSH: Two mysteries, quadratic residues still

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Now for the truly fun stuff as the result has implications for Goldbach's conjecture as it gives a reason for why you will always find primes for any composite, as there are only so many quadratic residues for all the primes up to  $C$ , right?

i think all integers up to  $c$  quadratic residues modulo some prime less than  $c$  if  $c$  more than 13...

if  $n=2$  then 2 is quadratic residue mod 7. if  $n=3$ , then mod 13. if  $n=4$ , then square, so mod every prime but two; if  $n=5$ , then 11.

if  $n>5$  and smaller  $c$ , look at  $n-1$  and  $n-4$ ; cannot both be powers of 2, since opposite parity and neither 1, so one is odd. if  $p$  is odd prime dividing  $n-1$ , then  $n = 1 \pmod p$  so square mod  $p$ ; if  $p$  odd prime divide  $n-4$ ,  $n=4 \pmod p$  so square mod  $p$ . either case  $n$  and  $p$  relative prime so  $n$  quadratic residue mod  $p$ . and  $p$  less than  $n$ , so  $p$  less than  $c$ .

so all integers up to  $c$  are squares mod some odd prime less than  $c$  if  $c$  more than 13 no?

reader

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