

Re: Looking for a surjection or \mathbb{R}^2

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I wrote:

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As before, identify \mathbb{R}^2 with \mathbb{C} , and let $p(z)=z^3-3z$. Then p is a 3-sheeted irregular branched cover of \mathbb{C} over \mathbb{C} , with critical points 1 and -1, and critical values $-2 = p(1) = p(-2)$ and $2 = p(-1) = p(2)$. The preimage $p^{-1}(\mathbb{R})$, call it G , is the union of \mathbb{R} and two (real) parabolas

which is of course wrong--with $z = x+iy$ as usual, G is the zero-set of $y(3x^2-y^2-1)$, so it's the union of \mathbb{R} and the two branches of a *hyperbola*.

Lee Rudolph

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