

Re: JSH: The "Published" paper he dosen't what you to know about.

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- *From:* "marcus_b" <marcus_bruckner@xxxxxxxxx>
 - *Date:* 18 Sep 2006 18:47:55 -0700
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Sue wrote:

Paper published and withdrawn paper by crank/crackpot James Harris exposes the "Over linterperations of Galois Theory" by mathematicians.
http://www.ne-plus-ultra.net/pubs/beckwith_factorization.pdf

ADVANCED POLYNOMIAL FACTORIZATION

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Abstract.

Algebraic method for determining distribution of factors within a polynomial factorization, which breaks through what was seen as a barrier from over interpretations of Galois Theory

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Advanced Polynomial Factorization Approached.

Determining the distribution of factors within irrational algebraic integers has long been considered impossible as it is not possible to do using Galois Theory. However a simple technique through the introduction of more variables makes it possible. To highlight the standard belief consider the algebraic integer roots of $x^2 + x - 5$.

While you know that the algebraic integer factors are themselves factors of

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5, can either not have non unit factors of 5? How do you know?

In looking to consider distribution of algebraic integer factors within a factorization I'll be using a more complicated example than $x^2 + x + 5$.

This paper will show, using basic algebraic methods, that given the factorization, in the ring of algebraic integers,

$$65x^3 - 12x + 1 = (a_1x + 1)(a_2x + 1)(a_3x + 1)$$

one of the a's is coprime to 5.

First I'll need a simple lemma to generalize beyond factors of a polynomial that are themselves polynomials.

Factorization Lemma:

Given a factor g of a polynomial $P(x)$, further defined as a factor for all x , which means that the value of g for a value 'a' of x is a factor of $P(a)$, within the ring of algebraic integers, there exists r and c such that

$$g = r + c$$

where $r=0$, or varies as x varies, and c is a factor of the constant term $P(0)$ and is itself constant.

Let $x=0$, then g must be a factor of $P(0)$, so at that point $c = g$.

If when x does not equal 0, $g = c$, $r=0$. If when x does not equal 0, $g = c$ there must exist r which varies with x . That is, $r = g - c$.

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As an example consider $\sqrt{x+1}$ which is a non polynomial factor of $x+1$, and while there are an infinity of irrational solutions consider the rational solution at $x=35$.

Then I have $\sqrt{35+1} = 6 = 5 + 1$; therefore when $x=35$, $g=6$, $r=5$, and $c=1$. But for different values of x , g and r will vary, while c will not.

Primary Argument.

Given

$$65x^3 - 12x + 1 = (a_1x + 1)(a_2x + 1)(a_3x + 1)$$

in the ring of algebraic integers. Let

$$P(m) = f^2((m^3f^4 - 3m^2f^2 + 3m)x^3 + (1 + mf^2)x^2 + u^3f)$$

Here f is a non unit, non zero algebraic integer coprime to 3 and x , and u a non unit, non zero algebraic integer coprime to f . Note $P(m)$ has a factor that is f^2 .

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That expression comes from expanding $(v^3+1)*x^3-3v*x*y^2+y^3$, using the substitutions

$$v = -1+m*f^2, \text{ and } y = u*f,$$

where additional variables provide an additional degree of freedom.

Now consider the factorization

$$P(m) = (a1*x + u*f)(a2*x + u*f)(a3*x + u*f)$$

where multiplying out shows that

$$a1*a2*a3 = m^3*f^6 - 3*m^2*f^4 + 3m*f^2 = f^2(m^3*f^4 - 3*m^2*f^2 + 3*m)$$

so

$$a1*a2*a3 = m*f^2*(m^2*f^4 - 3m*f^2 + 3).$$

Therefore, at least one of the a's cannot be coprime to m, and at least one of the a's must equal 0 when m=0.

(Note: The a's are roots of a monic polynomial with algebraic integer coefficients so they are algebraic integers.)

Notice that the constant term P(0) is given by $P(0) = f^2*(3*x*u^2 + u^3*f)$ and also that $P(0)/f^2 = 3*x*u^2 + u^3*f$, which is coprime to f.

Then I have the factor of P(m), g1, where $g1 = a1*x+u*f$, where here I also have that a1 is not coprime to m.

From my factorization lemma, I have that, when m =0, $g1 = c = u*f$, meaning f is a factor of the constant term.

Therefore, exactly two of the a's equal 0, when m =0, to get the factor f^2 in the constant term P(0), while one must not equal 0, or f^3 would be the factor.

Now as noted before in general P(m) has a factor that is f^2 , and separating that factor off, gives a constant term coprime to f; therefore, given $g1 = a1*x + u*f$ where with m = 0, g1 gives a factor of f it must have that same factor in general, proving that two of the a's have a factor that is f.

Therefore, one factor is coprime to f.

Now letting m =1, $f = \text{sqrt}(5)$, where I can let u=1 as its value doesn't change the a's,

I have

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$$(m^3 f^6 - 3 m^2 f^4 + 3 m) x^3 - 3(1 + m f^2) x u^2 + u^3 = 65 x^3 - 2 x + 1$$

which may be more easily seen from using

$$v = -1 + m f^2 = 4, y = 1 \text{ with } (v^3 + 1) x^3 - 3 v x y^2 + y^3.$$

Therefore, with the factorization

$$65 x^3 - 12 x + 1 = (a_1 x + 1)(a_2 x + 1)(a_3 x + 1)$$

one of the a's is coprime to 5, which shows where some of the algebraic integer factors distribute despite the factors being irrational.

Another version, different in detail, not co-authored by Beckwith, appears in a webzine called 'Chiaroscuro':

<http://www.etienne.nu/isis/Chiaroscuro8.pdf>

The date is July 2005. The first sentence is: "Over a hundred years ago subtle error crept into number theory."

A variant of Harris's deeply flawed argument involving constant terms of functions is still present.

Is this the version that was sent to the Annals of Mathematics?

Marcus.

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