

Re: A simple question?

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Jules wrote:

Actually, that quote

For example, the real numbers are not well ordered, but there is a well-ordering of the real numbers which is not the standard ordering.

came from my post. I meant that such an ordering exists, if one assumes the axiom of choice. I meant to use this simply as an example that a set need not be well ordered, even if a well-ordering of the set exists.

What does it mean for set not to be well ordered even though a well ordering of the set exists?

A better example is probably the set Z of integers. Z is certainly not well-ordered (it has no minimal element),

The standard ordering is not a well ordering, but that does not entail that the set is not well ordered. Maybe this is just a difference in how we use these phrases, but I say a set is well ordered iff there exists a well ordering of the set. So the fact that the standard ordering is not a well ordering doesn't contradict that the set is nonetheless well ordered.

but a well-ordering of Z can be explicitly described.

Okay.

I still want to know

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what the "natural" ordering of $P(\omega)$ is.

My impression is that what is being said in this thread is that there is no such thing as "the natural ordering of the power set of ω ".

MoeBlee

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