

Re: Cantor Confusion

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- *From:* Virgil <virgil@xxxxxxxxxxx>
 - *Date:* Fri, 16 Mar 2007 14:31:24 -0600
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In article <1174055000.972069.261630@xx>, mueckenh@xxxxxxxxxxxxxxxxxxx wrote:

On 16 Mrz., 15:15, Carsten Schultz <cars...@xxxxxxxxxx> wrote:

mueck...@xxxxxxxxxxxxxxxxxxx schrieb:

On 16 Mrz., 14:35, Carsten Schultz <cars...@xxxxxxxxxx> wrote:

mueck...@xxxxxxxxxxxxxxxxxxx schrieb:

On 16 Mrz., 01:31, Virgil
<vir...@xxxxxxxxxxx>
wrote:

In article
<1173954799.919385.61...@xx>, For even
binary trees
(where
even here
means all
paths are of
equal
length),

Only those are under
discussion here.

the number

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of paths
increases
exponentially
with
number of
levels
(lengths of a
path).
Adding 1 to
the number
of levels
doubles
the
number of
paths.

The
tree
is
continuous
because
its
nodes
are
connected
by
paths.

That is a
distinctly
non-standard
meaning for
"continuous"
in
mathematics.

It shows, however, that the
number of paths cannot
jump from finite to
uncountable.

Using a word does not constitute proof.

And indeed $\sup_{n < \aleph_0} 2^n = \aleph_0$
 $< 2^{\aleph_0}$,
so in this sense the function $\kappa \mapsto 2^\kappa$
is not continuous. If
you can prove (not claim!) by using your
tree that it is, then you will

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finally have succeeded in showing that ZF is inconsistent.

Have fun,

I had already quite a lot.

I can imagine.

The function of all cross sections, $f: n \mapsto 2^n$, is "continuous" in the sense that never a jump by more than a factor 2 can occur because the nodes of the tree are connected by an untearable network. The domain is the same as the range, namely \mathbb{N} . That is fact, not by claim but by construction of the tree. That's why I constructed it.

You constructed the tree to show that $2^{n+1} \leq 2 \cdot 2^n$? Well, that really must have been fun. Ok, I agree on this. Now we know a property of the function

$$\begin{aligned} f: \mathbb{N} &\rightarrow \mathbb{N} \\ n &\mapsto 2^n. \end{aligned}$$

This does not tell us anything about 2^{\aleph_0} .

\aleph_0 is not a natural number.

Are you just discovering that?

Don't mistake the infinite number of finite paths with infinite paths.

An infinite path corresponds to an infinite set of finite paths in the which the nodes of each path in the set are included as nodes in every longer path in the set. There is one such infinite path for each such maximal infinite set of finite paths and vice versa.

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And the union of the infinite set of finite paths, as set of nodes will be the set of nodes of the infinite path. And that is using the legitimate meaning of union as in ZF or NBG.

In the union of all finite trees every path has a finite length, given by a natural number of nodes. Presently we are considering the union of all such finite paths. (The union of all finite natural numbers is an infinite union – nevertheless this union contains only finite numbers.)

The mathematical union of the set of all finite paths is merely the set of nodes of the tree. But each infinite path requires a different infinite subset of the set of all finite trees, as described above.

So WM is faced with something like the power set of his set of all finite paths, not merely the set of finite paths itself. And WM cannot handle it.