

Re: Independent Random Variables

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In article <qqe13d5pjr851gqg0avk8ic7chka536ng@xxxxxxx>, David C. Ullrich <ullrich@xxxxxxxxxxxxxxxx> wrote:

On 6 Apr 2007 16:47:47 -0700, albert.koltai@xxxxxxx wrote:

- ◇ I am now taking a course in Probability Theory, and I am having
 - ◇trouble "visualizing" what do two independent random variables look
 - ◇like. The definition in terms of the cumulative distribution function
 - ◇or in terms of probability densities is clear enough, but when I am
 - ◇trying to imagine say, two or more real valued independent variables
 - ◇defined on the reals (with Borel sets as the sigma algebra) I am
 - ◇drawing a blank.
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- ◇ Could someone give me nontrivial examples of a set of real valued
 - ◇defined of the reals independent random variables?
 - ◇A general method of obtaining such --- nice enough to graph them ---
 - ◇random variables would be better.

I once read in some book that the notion of "independent variables" in probability has nothing to do with the "independent variables" that you find in calculus books. That was a lie – the two concepts are very closely related.

Assuming that you're talking about probability theory based on measure theory: Two random variables X and Y are independent if and only if the sample space can be realized as a `_product_` space, where the distribution of X is a measure depending only on one variable and the distribution of Y is a measure depending only on the other variable.

In general, a family of random variables are independent if, given any information about some of them, there is no information about the probabilities of events involving the others. This is

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how it is used; the usual characterization reduces the conditions which need to be checked.

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This address is for information only. I do not claim that these views are those of the Statistics Department or of Purdue University.

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