

Re: Separation, Power and Countability.

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- *From:* zuhair <zaljoahar@xxxxxxxxxx>
 - *Date:* Tue, 19 Jun 2007 22:25:52 -0700
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On Jun 20, 12:15 am, MoeBlee <jazzm...@xxxxxxxxxx> wrote:

On Jun 19, 9:36 pm, zuhair <zaljo...@xxxxxxxxxx> wrote:

On Jun 19, 11:05 pm, Keith Ramsay <kram...@xxxxxxx> wrote:

On Jun 19, 7:26 am, zuhair <zaljo...@xxxxxxxxxx> wrote:
|I asked for the proof of the following:
|For any set d that is a member of Pw and is undefinable what
|is the
|prove of d being equinumerous to w ?

Meaning, I suppose, how can one prove that each undefinable subset A of w is equinumerous with w .

If A is finite, then A is definable as $\{n : n \text{ is a natural number and } (n=a_0 \text{ or } n=a_1 \text{ or } \dots \text{ or } n=a_m)\}$ for some a_0, \dots, a_m .

If A is undefinable, then, A is infinite and each infinite subset of w is equinumerous with w . Let a_0 be the least element of A , and inductively let a_{k+1} be the least element of A not among a_1, \dots, a_k . Then a_i gives a 1-1 correspondence between A and w .

Re: Separation, Power and Countability.

Keith Ramsay

This depends on choice.

No, it doesn't; think about it for a moment.

it doesn't for this particular example since w is well ordered, I know. But I was talking about the bigger picture.

for example take PP_w , and let d be a member of PP_w that is not a member of P_w and let d be undefinable and uncountable.

Now what is the proof that $\exists f: P_w \rightarrow d$

of course I am speaking in a set theory without choice.

Zuhair

MoeBlee– Hide quoted text –

– Show quoted text –

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