

# Re: Separation, Power and Countability.

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- *From:* MoeBlee <jazzmobe@xxxxxxxxxxxx>
  - *Date:* Wed, 20 Jun 2007 10:37:32 -0700
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On Jun 20, 9:24 am, zuhair <zaljo...@xxxxxxxxxx> wrote:

On Jun 20, 12:54 am, MoeBlee <jazzm...@xxxxxxxxxxxx> wrote:

for example take  $PP_w$ , and let  $d$  be a member of  $PP_w$  that is not a member of  $P_w$  and let  $d$  be undefinable and uncountable.  
Now what is the proof that  $\exists f: P_w \rightarrow d$

what is that: the question is what is the proof that  $\exists f: P_w \rightarrow d$ ,  $f$  is injective).

Yes, you need to say "f is injective" if that is what you mean.

Anyway, without the continuum hypothesis, I don't know why all such  $d$  are equinumerous with  $P_w$ . Maybe they are, but I don't know why one would think that they are.

well my question is of course without the continuum hypothesis. But let's assume the continuum hypothesis  
SHOW me an injective function from  $P_w$  to  $d$ , Remember  $d$  is an uncountable and undefinable subset of  $P_w$ .

First, if  $d$  is not defined as a particular set, then, it is not clear to me what we can show any PARTICULAR function that has  $d$  as a superset of the range. Second, even WITH the generalized continuum hypothesis (I meant 'generalized' in my first mention also), I don't know that there is a proof that  $P_w$  dominates  $d$ . (With the generalized continuum hypothesis,  $d$  is either equinumerous with  $P_w$  or with  $PP_w$ .) Third, just to note, now you've been explicit that  $f$  needs only to be an injection (not necessarily a bijection).

Re: Separation, Power and Countability.

More basically, I don't know what you think is at stake in showing that  $d$  is dominated by  $P_w$ .

of course I am speaking in a set theory without choice.

Then you're not allowing the generalized continuum hypothesis.

MoeBlee

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