

Re: Ultimate debunking of Cantor's Theory

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- *From:* Calvin <crice5@xxxxxxxxxxxxxxxx>
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On Jul 13, 2:03 am, "Peter Webb"
<webbfam...@xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx> wrote:

What Prog said is quite true. He just picked an example which (whilst correct) is probably a little bit too clever.

He hasn't claimed that you can write down a list of all Reals in base 2. He claims that the Cantor diagonal argument cannot be used in base 2 to prove this.

Here is a somewhat clearer example.

Imagine the list is:

- a(1) = 0.011111 ...
- a(2) = 0.01
- a(3) = 0.001
- a(4) = 0.0001
- .
- .

Form the diagonal by flipping bits. You get

cantor diagonal = 0.1000000...

But 0.0111... is the same number 0.1 (unless you also believe that 0.999... <> 1), and so the Cantor diagonal does appear on the list.

Now we all know that the list above doesn't contain every Real, but the Cantor diagonal construction doesn't itself prove this to be true.

(His example was a "bit too clever" because he set $a(2) = a(3) = a(4) \dots$, which is quite valid but obscures his central argument).

My problem with what he did is not a failure to understand that 0.0111... is the same number as 0.1; I accepted that immediately.

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My problem with it is that he produced a CONTRIVED list, flipped the diagonal and said that the new number thus produced is indeed already in the list. So what?

That's not the sort of thing Cantor's argument is. He takes a traditional reductio ad absurdum approach and 'assumes' that what he wants to prove is not true. If it were not true, then a countable list of decimal (or binary) expansions of the reals between 0 and 1 could exist. He didn't say how such a list might be generated. How could he? Why would he? He wants to show that the existence of such a complete list is impossible.

To make a simple analogy, if you are proving that there is no rational number the square of which is 2, you assume the contrary and posit integers p and q in lowest terms, q not 0, for which the square of p/q is 2. You don't claim to know what p and q would have to be. That would be outrageously absurd, since your motive is to prove that they don't exist as posited.

I could be very much in sympathy with a complaint against Cantor's diagonal argument that said it is not acceptable to operate on the assumed impossible list to the extent that he does in order to 'show' that such a countable list cannot be complete. I've always been uneasy about that. But the sort of approach that Proginoskes uses to 'refute' Cantor in the case of a list of binary forms of the reals is an insult to everyone's intelligence, it seems to me.

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