

## Re: \*\* says: Definition: $\sum\{i \text{ in } \mathbb{N}\} i = 0$

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  - *Date:* Mon, 16 Jul 2007 16:02:09 +0200
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G. Frege wrote:

On Mon, 16 Jul 2007 15:08:25 +0200, Han de Bruijn  
<[Han.deBruijn@xxxxxxxxxxxxxxxx](mailto:Han.deBruijn@xxxxxxxxxxxxxxxx)> wrote:

But I'm fascinated by the fact that there exist NO other shapes of the  $\sin(x)/x$  rather than the  $\text{sinc}(x)$  function in the real (physical) world. Only this one is relevant:

$$\begin{aligned}\text{sinc}(x) &= \sin(x)/x \text{ for } x \neq 0 \\ &= 1 \text{ for } x = 0\end{aligned}$$

And I'm asking the community to explain this (not by coincidence) fact.

It's just that this is the ONLY possible extension of  $x \mapsto \sin(x)/x$  from (the domain)  $\mathbb{R} \setminus \{0\}$  to  $\mathbb{R}$  such that the resulting function is continuous (and even differentiable) on (all of)  $\mathbb{R}$ .

You know, there's an old saying "Natura non facit saltus" ("nature does not make (sudden) jumps"), though I'm in doubt if this statement can still be considered to be true in the light of modern quantum mechanics.

See:

[http://en.wikipedia.org/wiki/Natura\\_non\\_facit\\_saltus](http://en.wikipedia.org/wiki/Natura_non_facit_saltus)

How about "physical" functions which are defined at a closed interval of real numbers? Are they always continuous there? What do you think?

Han de Bruijn

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