

Re: Bringing back an old tetration curiosity?

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- *From:* mike3 <mike4ty4@xxxxxxxxxx>
 - *Date:* Wed, 19 Sep 2007 23:32:35 -0700
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On Sep 17, 3:31 pm, theronr...@xxxxxxxxxx wrote:

On Sep 17, 9:45 pm, mike3 <mike4...@xxxxxxxxxx> wrote:

On Sep 17, 11:22 am, theronr...@xxxxxxxxxx wrote:

On Sep 17, 6:12 pm, theronr...@xxxxxxxxxx wrote:

<snip>

After rethinking I think that the above statement is a bit speculative. However I'm sure that there is no continuous $f: (-2; +\infty) \rightarrow \mathbb{R}$ that satisfies (1), (2) and (3). Here is why:

<http://img403.imageshack.us/img403/1466/sqrrtetrxjx1.png>

This is a 5000x5000 plot of $f(x)$ for $-1 \leq x \leq 0 \leq y \leq 1$.

Theron

This is interesting. There appears to be a gentle undulation in it, oddly enough. It's intriguing to examine that in light of a graph of $^x(0.1)$ on the integers, which oscillates quite a bit.

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I'd be curious to see your program, to root out various sources of approximation error, for example, though.

The branching doesn't look to me as a side effect of possible rounding errors. I can send you the C source code of the program, but I would like an independent verification of the result. If your program produces the same result (the same branching) then this will reaffirm the result. It is not difficult to write such a program.

Theron

How did you write the program, exactly? That's why I'd like to see it. My program just mirrors and recurses starting with an integer and then plots all the iterates on the graph. This gives a more-or-less sparse graph, though. However on closer inspection it seems you might be right — there are points on the graph that make it seem sort of "fuzzy" (in the way that would suggest the behavior you observed). Decreasing precision of the numbers used did not appear to change the graph. Of course I didn't change the `_format_` of the number to something (that might, say, handle overflows, for example, differently) else, however.

This would suggest then that the tetrational function is `_close_` to symmetrical but not exactly so. I'd be curious to know if the difference between the value of $^{0.5}\sqrt{2}$ obtained using this method and that obtained by assuming it is the square tetra-root of $\sqrt{2}$ is small enough that perhaps the `_correct_` curve for $\sqrt{2}$'s tetrational function would be able to pass through it at 0.5...

Regardless, the symmetry is obviously `_close_`, but no `_cigar_`. I'd be curious to hear some more opinions from others here on this group. It seems though like the guy's original idea, at least in that form, is likely another dead end...

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