

# Re: 4 real periods

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- *From:* hagman <[google@xxxxxxxxxxxxxxx](mailto:google@xxxxxxxxxxxxxxx)>
  - *Date:* Fri, 21 Sep 2007 13:13:47 -0700
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On 21 Sep., 20:59, tommy1729 <[tommy1...@xxxxxxxxxx](mailto:tommy1...@xxxxxxxxxx)> wrote:

david wrote:

On Thu, 20 Sep 2007 16:54:44 EDT, tommy1729  
<[tommy1...@xxxxxxxxxx](mailto:tommy1...@xxxxxxxxxx)>  
wrote:

David C Ullrich wrote

On Wed, 19 Sep 2007 09:35:05 EDT,  
tommy1729  
<[tommy1...@xxxxxxxxxx](mailto:tommy1...@xxxxxxxxxx)>  
wrote:

consider the  
set of  
functions  $R$   
 $\rightarrow R$   
with  
 $F(x) = A +$   
 $B + C + D$

where  $A, B$   
,  $C, D$  have  
4 real  
periods and

satisfy  $R$

$\rightarrow R$

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$$A = a_0 + a_1 \sin(P_1 x) + a_2 \sin(2 * P_1 x) +$$

a\_3

$$\dots + A_1 \cos(P_1 x) + A_2 \cos(2 * P_1 x) + A_3 x) + A_3 \dots$$

$$B = b_0 + b_1 \sin(P_2 x) + b_2 \sin(2 * P_2 x) +$$

b\_3

$$\dots + B_1 \cos(P_2 x) + B_2 \cos(2 * P_2 x) + B_3 x) + B_3 \dots$$

ETC ( real fourier series )

1) given a function  $G(x) \mathbb{R} \rightarrow \mathbb{R}$ , how do we

decide

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if

it belongs to  
this set ?

2) how do  
we find the  
4 real  
periods  
P\_1, P\_2,

P\_3

and P\_4 ?

3) how do  
we find the  
coefficients  
of A B C  
and

D

?

(\*)

(\*) knowing  
the answer  
to 2  
questions  
also

solves

the

3rd.

(note: of  
course  $G(x)$   
is not given  
as the sum

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of 4

fourier  
series nor  
are its  
periods  
given in

advance)

regards  
tommy1729

well ? where are the  
calculus experts now ?

The calculus experts are pretty certain that  
since  
you insist on spouting nonsense about utterly  
elementary  
topics in complex analysis there's very little

point

in trying to explain the theory of

"almost-periodic

functions" to you.

dont speak for others David.

what you really want to say is you dont understand

it either hmm

spouting nonsense like  $\int x \, dx = 2x + 1$

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oh no , wait thats your equation.

you are a very strange "prof" David.

1) you wrote  $\int x dx = 2x + 1$  for example  
(there are similar "math demonstrations" )

but hey lets disregard that ,

2) when the questions become hard , you ignore the  
thread or you say it is trivial...

3) ... without solving it !!!

seems like you cant do the math , or you are not  
very good at helping people with it.

you even refuse to give a decent answer.

if you cant do math or you refuse to help people  
with math , that makes you a very "special type" of  
prof.

even if i only assume the second.

but whats even worse:

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you have no idea what this is all about dont you ?

if the question is so simple , why dont you give the formula for the 4 periods ?

you refer to " almost periodic functions"

if you truly are a prof , i assume a prof in physics.

why ? because only in physics this could work out.

in math , this is a mistake.

it works out for problems like n-body problems or quasicrystals, because they can be solved with the math of almost periodic functions ...

because they ARE almost periodic functions

however my questions was quite different.

definition of almost periodic function :

$F(x)$  is almost-periodic if every sequence of

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translates of  $F(x)$  has a uniformly convergent subsequence.

almost periodicity is a property of dynamical systems that appear to retrace their paths through phase space, but not exactly.

OK, I'll read the rest of that wikipedia article as well.

if we consider functions based on time then a theorem of Kronecker ( yes kronecker THE ENEMY OF CANTOR !! doing math cantor could not ! ) from diophantine approximation can be utilized to show that a particular configuration that occurs once, will recur to within any specified accuracy in finite time.

(haha you yourself lead me to a theorem of kronecker while you are a cantorian :p)

the problems are that this does not apply well with my questions because of at least 2 reasons :

1) for almost periodic functions we have the condition

$$\text{ABS } [F(t) - F(t + P)] < B$$

where abs is the absolute value , t is time and the

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real parameter of the function,  $P$  is the almost period and  $B$  is finite real number.

Apparently you didn't read the article thoroughly enough. With your definition I could take  $F$ =characteristic function of rationals,  $B=1.1$ ,  $P=17$  and could obtain that  $F$  is almost-periodic with almost period 17. Instead, the definition should be that for every  $B>0$  you can find a  $P>0$  (thus depending on  $B$ ) such that etc.

compare with my question ; 1) the restriction  $B$  is

not present, my fourrier series can go to infinity  
!!!

so the condition of almost periodic functions is not  
matched !!

(it is usually so in physics because we have finite  
distance as in  $n$ -body problems and similars )

so  $B$  is not matched, and neither is  $P$  as shown in 2)

2) since we have 4 periods we have a lot of periods  
; therefore none of them can be dominant so we dont  
have an approximation to a certain period  $\rightarrow P$   
cannot be determined consistantly.

3) well ill spare you that, not to embarras you to  
much :p

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perhaps you were thinking what about quasiperiodic

functions then ??

- 1) not invented by quasi despite he understands them
- 2) don't work either

i guess you will have to invent something new to

analyse

4-periodic functions

Once again, you talk about mathematics that you don't have any understanding of.

now i showed you didn't :)

You should really learn to

stop doing that. The sum of two (continuous) periodic functions is almost periodic.

i agree with that :-)

That's a fact, even

if it's not mentioned in the place where you found the (garbled) definition above.

lol, i agree with you :)

read the title david :

FOUR periods

not just 2 ...

you know  $2 + 2 = 4$  so just adding 2 periods is insufficient.

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why cant you just admit you are wrong.

or give the solution

you never do either.

because you cant solve it , and neiter admit it.

but hey look on the bright side i agree on what you said ....

yet it is not relevant of course

you really have to do better than this if you want to give the solution or show that i am wrong.

answering a 4 period question with a 2 period answer ...

lol

perhaps you want to add 2 almost periodic functions and call them ullrich-almost-5-periodic-functions to tackle the problem...

and it works fine with the above definition.

perhaps ullrich-almost-3-periodic-functions  
or ullrich-almost-5-periodic-functions

tommy1729  
"tommy is tommy, crazy but crazy like a fox"  
"polysigned is the future"  
"what is  $g(g(x))=f(x)$  to easy for you ? "  
"math is bigger than physics"  
"tommy is undecidable"

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David C. Ullrich

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David C. Ullrich

regards funny david  
tommy1729

Assume A has the property  
for all  $\epsilon > 0$ : exists  $P > 0$ : for all  $x$ :  $|A(x) - A(x+P)| < \epsilon$   
(aka. almost periodic)

and B is continuous and periodic with period Q.

Then  $C := A+B$  is almost periodic.

Proof:

Assume  $\epsilon > 0$  given.

Let  $\epsilon_n$  be a sequence of positive numbers converging to 0.

For each n, there is an  $\epsilon_n$ -almost period  $P_n$  of A.

The sequence  $P_n \bmod Q$  has an accumulation point R.

Wlog.  $P_n \bmod Q$  converges to R.

Let  $k_m$  be a sequence of positive integers such that

$k_m * R \bmod Q$  converges to 0 (or Q if you like).

For each m, we have  $\epsilon_n < \epsilon / (2 * k_m)$  for n big enough.

By taking a subsequence of the  $P_n$ , we may assume wlog. that  
 $\epsilon_n < \epsilon / (2 * k_n)$  for all n.

Again by taking a subsequence of the  $P_n$  (but not the  $k_n$ ),  
we may assume that  $k_n * P_n \bmod Q$  converges to 0 (i.e. the  
difference between  $k_n * P_n$  and the closest integer multiple of Q  
converges to 0).

Observe that  $k_n * P_n$  is an  $\epsilon/2$ -almost period of A  
per telescope summing.

Next, the Q-periodic functions  $B_n(x) := B(x) - B(x + k_n * P_n)$   
converge pointwise to 0.

The  $B_n$  are clearly equicontinuous and uniformly bounded.

Hence, by Arzela-Ascoli, some subsequence converges uniformly  
(of course also towards the pointwise limit)

Wlog.  $B_n \rightarrow 0$  uniformly.

Thus, for n big enough,  $|B_n(x)| < \epsilon/2$  for all x.

$|C(x) - C(x + k_n * P_n)| \leq |A(x) - A(x + k_n * P_n)| + |B(x) - B(x + k_n * P_n)|$   
 $< \epsilon/2 + \epsilon/2 = \epsilon$  for all x.

Thus C is almost periodic. QED

(Gee, I'm so glad  $\epsilon/2$  worked out. I hate it when you  
note that you have to go back and replace all  $\epsilon/2$  by  $\epsilon/3$  ;) )

Corollary: The sum for finitely many continuous periodic functions  
is almost periodic.

Proof: trivial induction.

I'm sorry that my proof is so lengthy and unelegant, but

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I have read this thread and especially the definition of almost periodic just 10 minutes ago and I'm rather algebraist than analyst. Someone who has considered the original problem thoroughly for some time and can tell immediately when D. Ullrich is wrong, could surely make that proof more stringent.