

Re: Bringing back an old tetration curiosity?

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- *From:* "I.N. Galidakis" <morpheus@xxxxxxxxxxxxxx>
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mike3 wrote:
[snip]

For example, one should expect $x^{(0.49999\dots)}$ to be exactly $x^{(0.5)}=x^{(1/2)}$.

And it is, since the function is defined using *real* arguments, not "decimal" arguments. It's defined on the set \mathbb{R} of real numbers, like I said, not on the set \mathbb{D} of decimal expansions.

In order to define a function with a *real* argument, you have to tell me what the function *does* to the argument (preferably in terms of Cauchy sequences and limits). I'll make it easier for you: You have to tell me **FIRST** what the function does to a *rational* argument, like m/n .

I asked you "what does the function do for $x^{(2/30)}$ "?, and you agreed to, "let $y=m/n$ be the corresponding value and then evaluate x^y ".

I responded: "This is an ambiguous way to tell me what the function does, because y might not have a unique decimal representation".

If you cannot tell me what the function does to a *rational* argument, you cannot tell me what it does to a (generally) real argument.

Sorry, I am through arguing. You don't see the problem.

[snip]

—
I.N. Galidakis