

## Re: Bringing back an old tetration curiosity?

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*Source:* <http://sci.tech-archive.net/Archive/sci.math/2007-09/msg04822.html>

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- *From:* mike3 <mike4ty4@xxxxxxxxxx>
  - *Date:* Fri, 21 Sep 2007 18:34:58 -0700
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On Sep 21, 5:20 pm, "I.N. Galidakis" <morph...@xxxxxxxxxxxxxx> wrote:

mike3 wrote:

[snip]

For example, one should expect  $x^{(0.49999\dots)}$  to be exactly  $x^{(0.5)}=x^{(1/2)}$ .

And it is, since the function is defined using *real* arguments, not "decimal" arguments. It's defined on the set  $\mathbb{R}$  of real numbers, like I said, not on the set  $\mathbb{D}$  of decimal expansions.

In order to define a function with a *real* argument, you have to tell me what the function *does* to the argument (preferably in terms of Cauchy sequences and limits). I'll make it easier for you: You have to tell me **FIRST** what the function does to a *rational* argument, like  $m/n$ .

Yes!

I asked you "what does the function do for  $x^{(2/30)}$ "?, and you agreed to, "let  $y=m/n$  be the corresponding value and then evaluate  $x^y$ ".

Yes, since  $m/n$ ,  $y$ , are all referring to the same abstract number, in fact from the abstract standpoint of numbers *they are exactly the same*! That abstract number, the number "itself", is what a function like this acts upon.

Re: Bringing back an old tetration curiosity?

I responded: "This is an ambiguous way to tell me what the function does, because  $y$  might not have a unique decimal representation".

If you cannot tell me what the function does to a *\*rational\** argument, you *\_cannot\_* tell me what it does to a (generally) real argument.

I know, you have to define what it does to the rational argument. But that means we define it *\*for an element in  $\mathbb{Q}$ \**, not for an element in the set of quotient expressions.  $2/30$  is the exact same element of  $\mathbb{Q}$  as  $1/15$ , so the function's value for the two must be *\*exactly the same\**! Why can it not be? The two are just two ways of writing the same rational number in  $\mathbb{Q}$ .

Sorry, I am through arguing. You don't see the problem.

I'm trying to see the problem.

[snip]

—

I.N. Galidakis