

Re: Is CW a local property?

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- *From:* sanchopancho80@xxxxxx
 - *Date:* Sun, 07 Oct 2007 08:46:29 -0700
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On 6 Okt., 11:51, Keith Ramsay <kram...@xxxxxxx> wrote:

On Oct 5, 4:04 am, sanchopancho...@xxxxxx wrote:
|can anyone help me to show that the Long-Line is not a CW complex but
|a 'local CW complex' in the sense of the first post?

Since each point on the long line has an open neighborhood homeomorphic to an open interval on the real line, the latter is easy.

The long line doesn't have a homeomorphic copy of the interior of B^n for $n > 1$, so if it were a CW complex, it would be a 1-frame. Suppose it is. The points in the 0-frame can't have an upper bound because there would be no way to glue a 1-cell so that it included any of the points above the upper bound. So there have to be uncountably many points in the 0-frame. It's only possible to connect a point in the 0-frame to two others, so only countably many points in the 0-frame can be path-connected. But the long line is path-connected. Details need to be filled in.

Keith Ramsay

Hello,
thank you! The long line isn't a compact space. Is the question above trivial for compact spaces?
Greetings
Sancho