

# Re: #326 Counting an infinite set versus a finite set ; new textbook: Mathematical Physics (Reals & Counting Numbers/AP-adics Primer) for age 6 years onward

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Source: <http://sci.tech-archive.net/Archive/sci.math/2007-11/msg03658.html>

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- From: "Jesse F. Hughes" <jesse@xxxxxxxxxxxxxx>
  - Date: Mon, 19 Nov 2007 07:23:58 -0500
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a\_plutonium <a\_plutonium@xxxxxxxxxxxxxx> writes:

If I start counting at 0, I get to 1 at the same time as I get to  $10^0$ .

I get to 2 before I get to  $10^1$ .

I get to 3 before I get to  $10^2$ .

I get to 4 before I get to  $10^3$ .

and so on, but I get to  $10^{\{999\dots998\}}$  before I get to  $999\dots999$ .

(The above you just conceded.)

I conceded not because of your argument, although it hastened it, for I conceded because I have the illogic that  $999\dots99999 + 1 = 10000\dots00000$

which is (pi) the South Pole and yet that cannot be consistent with  $10^{9999\dots99999}$  which is also the South Pole since it has one more digit place value than  $9999\dots99999$  itself.

So it is not your argument that force me to concede although it helped to hasten.

Whatever.

[...]

Thus, there is some  $n$  such that

If I start counting at 0, I get to  $n$  before I get to  $10^{n-1}$ , but  
I get to  $10^n$  before I get to  $n+1$   
(or maybe at the same time).

Do you agree with the above? If so, then what follows is an obvious consequence.

As lwalke3 pointed out, this would mean:

I get to  $n$  before  $10^{n-1}$ ,  
to  $10^{n-1}$  before  $10^n$ ,  
to  $10^n$  before or at the same time as  $n + 1$

and thus, there is at least one number between  $n$  and  $n + 1$ .

No, I buy none of that.

Okay, then you're just too broke to reason with.

You claim that every AP-adic aside from zero has a predecessor, yes?  
And that, starting at zero and adding one repeatedly, we will eventually reach any AP-adic?

Let  $P$  be the property "We count to  $n$  before we count to  $10^{n-1}$ ." We know that  $P$  is true at  $n=1, 2, 3$ . We know it is false at  $n = 999...999$ .

Now, I claim there is some  $n$  such that  $P(n)$  is true, but  $P(n+1)$  is false. You claim not. Let's suppose you're right. Then it follows that, if  $P(n)$  is true, so is  $P(n+1)$ .

Start counting at 1 and we get:

- 1:  $P(1)$  is true.
- 2:  $P(2)$  is true because  $P(1)$  is true.
- 3:  $P(3)$  is true because  $P(2)$  is true.
- 4:  $P(4)$  is true because  $P(3)$  is true.

and so on. Each time we reach a new number  $n$ ,  $P(n)$  must be true, since it was true at the predecessor. According to you, eventually, we reach  $999...9997$  by counting and thus we see:

- $999...99997$ :  $P(999...99997)$  is true because  $P(999...99996)$  is true.  
 $999...99998$ :  $P(999...99998)$  is true because  $P(999...99997)$  is true.  
 $999...99999$ :  $P(999...99999)$  is true because  $P(999...99998)$  is true.

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Oops!

Thus, what I said must be correct. There is a number  $n$  so that  $P(n)$  is true and  $P(n+1)$  is false.

I've wasted enough time on this obvious point to continue, I reckon.

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Jesse F. Hughes

"Certainly he who can digest a second or third fluxion need not, methinks, be squeamish about any point in divinity."

George Berkeley, 1734

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