

# Re: Fractional Transforms

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- *From:* David C. Ullrich <dullrich@xxxxxxxxxxx>
  - *Date:* Tue, 16 Dec 2008 05:23:09 -0600
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On Tue, 16 Dec 2008 16:20:10 +1100, "rancid moth"  
<rancidmoth@xxxxxxxxxxx> wrote:

"David C. Ullrich" <dullrich@xxxxxxxxxxx> wrote in message  
<news:amgdk4h906qlra8m60tgiqisbn5nkgs7ka@xxxxxxxxxxx>

On Mon, 15 Dec 2008 14:05:57 -0600, Robert Israel  
<israel@xx> wrote:

David C. Ullrich <dullrich@xxxxxxxxxxx> writes:

A few days ago I decided there was no point, considering the audience, in pointing out that the existence of a  $T$  with  $L = T^2$  is clearly impossible if we interpret things very strictly. We have  $L: X \rightarrow Y$  where  $X$  and  $Y$  are very different spaces of functions. If  $T$  were a functional square root of  $L$  then we'd need to have somehow  $T: X \rightarrow Z$  and also  $T: Z \rightarrow Y$ ; if we take  $T$  to have a well-defined domain and co-domain then it follows that  $X = Y$ . Of course this doesn't quite rule out the existence of some kernel that does the job at least formally.

On the other hand there are spaces  $X$  such that  $L: X \rightarrow X$ . For example, let  $X$  be the space of continuous functions  $f$  on  $(0, \infty)$  such that  $x^{1/2} f(x)$  is bounded.

## Re: Fractional Transforms

Heh, very good – I considered the possibility of such an X existing but didn't think of this simple example.

(Readers who are wondering why this X has that property should contemplate the Laplace transform of  $1/t^{1/2}$ ...)

[cut]

Yes. i was wondering about that.

Also – what do you mean "..there was no point, considering the audience..."

I said there was no point, referring to a time in the past when you were not part of the audience.

I know i'm a little wayward with my mathematics, but generally i'm ok and get there in the end...or at least i thought i was ok.

At the very least i thought i was polite enough to post and get responses. perhaps not.

??? You got a response. From me.

David C. Ullrich

"Understanding Godel isn't about following his formal proof. That would make a mockery of everything Godel was up to."  
(John Jones, "My talk about Godel to the post-grads."  
in sci.logic.)