

## Re: GPS calculations

**Source:** <http://sci.tech-archive.net/Archive/sci.physics.relativity/2004-09/7287.html>

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On Tue, 28 Sep 2004 14:49:01 -0500, EJP <nospam@hackers.are.bad> wrote:

>xxein wrote:

>> *For those confused by 46 us/day and 38 us/day, It depends on wether  
>> you think the satellites orbit once a day or twice a day.*

>>

>> *It seems there is a lot of confusion both on this ng and the general  
>> science archives.*

>>

>> *End.*

>

>*There is no confusion amongst those who know what they're talking  
>about. The correction is 38 usec a day, based on a perturbative  
>treatment which allows you to separate the "SR" and "GR" compoenents.  
>If you do this, you get a 45 usec advance from the gravitational  
>potential difference and a 7 usec slowing form the SR component,  
>giving a net correction of 38 usec. This was calculated \*long\*  
>before the satellites were launched and match observation exactly.*

>

>*Since the orbital period of GPS satellites is about 12 hours,  
>the correction per period is about 19 usec. I'm not sure  
>where your 46 usec comes from, except that it's close to the  
>45 that one gets from a partial calculation.*

>

>*The calculation is actually pretty simple. I've appended it  
>below. This version is a bit long because I was arguing with  
>some kook that claimed all sorts of "extra" factors had been  
>added, and I was showing that you can calculate the whole thing  
>if you know the altitude and period of the satellite and  
>the radius of the Earth.*

>

>  $-E$

>

>

>=====Details of GPS Calculation=====

>*The altitude of the GPS sats are about 20,000 km, so their  
>radius is 27,000 km. The observed period is 12 hours. From this you  
>can work out that the velocity is*

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>  
>  $v = 2\pi R/T = 3.93 \times 10^3 \text{ m/s}$   
>  
> This means that  $\beta = v/c = 1.31 \times 10^{-5}$ . The velocity at the  
> surface  
> of the earth is negligible compared to this, so the SR clock correction  
> would come from  
>  
>  $\gamma = 1/\sqrt{1-\beta^2} \sim 1 + .5\beta^2 \sim 1 + (8.5 \times 10^{-11})$   
>  
> so the orbiting clock would tick "slowly" by  $1/\gamma$ , or a fractional  
> change of  
>  
>  $8.5 \times 10^{-11}$   
>  
> and the clock would lose  $(86400) \times (8.5 \times 10^{-11}) = 7 \times 10^{-6} \text{ s/day}$   
>  
>  
> Now, move on to GR. Use  
>  
>  $v = \sqrt{GM/R}$  to get  $GM = 4.2 \times 10^{14}$   
>  
> The GR gravity-only time dilation "gamma" is (look it up)  
>  
>  $\gamma = 1/\sqrt{1 - 2GM/(Rc^2)} \sim 1 + GM/(Rc^2)$   
>  
> So the difference between a clock ticking on Earth ( $R=R_e=6.7E6$ ) and one  
> ticking in orbit  
> ( $R=R_o=27E6$ ) would be  
>  
>  $1 + GM/(R_e c^2)$   
> -----  $\sim 1 + (GM/c^2)(1/R_e - 1/R_o)$   
>  $1 + GM/(R_o c^2)$   
>  
> since the earth clock is deeper in the gravitational well, it would tick  
> slowly and relative to it, the GPS clock would tick fast by a factor  
>  
>  $(GM/c^2)(1/R_e - 1/R_o) = 5.23 \times 10^{-10}$   
>  
> so the clock would gain  
>  
>  $86400 \times (5.23 \times 10^{-10}) = 45 \times 10^{-6} \text{ s/day}$   
>  
> so the net gain would be  $45 - 7 = 38$  microseconds, which is (strangely  
> enough) EXACTLY the value they use, see  
> <http://www.phy.syr.edu/courses/PHY312.98Spring/projects/GPS/GPS.html>  
>

So what is it about movement or gravity wells that actually affects the way a clock ticks?

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You CDEFs all talk crap.

Just because light increases speed and incurs a doppler shift as it falls down a gravity well, you think 'clock ticks' do the same.

Maybe PA's famous tick fairies are at it again....!

HW.

[www.users.bigpond.com/hewn/index.htm](http://www.users.bigpond.com/hewn/index.htm)