

Re: How much energy required to evaporate one liter of H₂O ?

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In sci.physics, tj Frazir

<GravityPhysics@webtv.net>

wrote

on Tue, 20 Jul 2004 15:34:31 -0400

<29894-40FD73C7-158@storefull-3212.bay.webtv.net>:

- > *Boil it and you will need 100 times the energy by placing a flame under*
- > *the can than if you used that energy to run a vacuum pump .*
- > *A 60 watt vacuum pump will evaporate a gallon on water in less time*
- > *than a burner on the stove could boil the water dry.*
- > *IF you just let the water evaporate by its self then it cost you no*
- > *energy.*
- > *A solar furnace boiler running a steam engine*
- > *that runs a vacuum pump might or might not be better.*
- > *The deck can get rid of a gallon of water in 60 seconds so surface*
- > *area will be a large factor.*
- > *A tube boiler uses surface area per flame area .*
- > *IF its in a radiator it might take all the energy you can dump in and*
- > *not boil .*
- > *NOT very much;;; to,,, all the energy you want.*
- >

An interesting problem, that.

Let's see... Numbers. I need numbers.

[1] Take a liter of water (1000 cc, 1 kg) at 300 K. Vaporization energy at STP is 2.26×10^6 J/kg. Presumably vaporization energy at 300K is about the same. Atmospheric pressure is assumed at 101350 Pascal (= $\text{N/m}^2 = (\text{kg m/s}^2)/\text{m}^2$ or $\text{kg}/(\text{m s}^2)$).

[2] Let the sun shine in! Assuming all of the energy is used to vaporize and the water is carried away by a constant breeze, the amount of energy needed would be, as it turns out, 2.26×10^6 J.

[3] The vapor pressure of water at 300K = 27.3C is about 4,000 Pascal.

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[4] If one wants to boil the water, one must heat it to 373K.

It takes 1 kcal to heat 1 kg of water 1 degree; 1 kcal = 4180 J.

Therefore the amount of energy required for this step is $4180 * 73 = 305,000$ J. Total cost to put the water on a burner and watch it boil away dry: $2.565 * 10^6$ J.

This should be enough.

The first problem is computing the size of that water vapor cloud.

Guy-Lussac gives us:

$$V = nRT/P = (1 / 0.018) * 8.3144 * 300 / 101350 = 1.137 \text{ m}^3.$$

The second problem is computing the amount

of air needed in that breeze. We'll need to move at least

$1.137 * (101350 - 4000) / 4000 \text{ m}^3 = 27.67 \text{ m}^3$ of dry air across that water surface, and then dispose of the humid air.

The mass of this dry air is computable via Rydberg's

Constant, and a mole of air weighs about 29 g.

Total mass: $n = PV/(RT) = 101350 * 27.67 / (8.3144 * 300) = 1124.3$ kg.

More than a ton of air?! Woof.

If we assume the water's in a cubical vessel (0.1 m deep, 0.01 m² in area), we'll be moving a "tape" of air across that surface. This will probably be a fairly thick tape for minimum energy consumption, further exacerbated by the necessity of pushing the water bottom up as it evaporates (a total energy of $1/2 * 1 \text{ kg} * 0.1 \text{ m} * 9.805 \text{ m/s/s} = .49$ J, so that's not very much). We also need to consider that the water gains energy as it moves up: $E = mgh$. That's probably even less.

If we assume a tape thickness of 0.1 m (the width is of course 1 m to cover the water cube), we get a tape length of 276.7 m. After passing over the water the tape will be sopping wet, and the water in each section of the tape would have been raised 0.05 m on average. Total energy gained here: $0.05 * 9.805 * 1 = 0.49$ J again. Woo.

We now seal the cube in a container of size 1.137 m³ (for purposes of simplicity, the cross-section in a certain direction is 1 m², yielding dimensions of 1m x 1m x 1.137 m) and start pumping. We assume the ability of a certain filter to keep the air going to the pump absolutely dry, and sufficient controls/heat to keep the water at 300 K. In short, all the water will do in this experiment is transform from liquid to gaseous.

We pump out enough air to reduce the pressure from 101350 to 4000. That's equivalent to stretching a piston from 1.137 m

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to $1.137 * 101350/4000 = 28.81$ m. The pressure on one side of this piston is $101350 * x / 28.81$ (where x is the distance from the other wall of the piston's face); the pressure on the other side is 101350. The amount of work required is then, by simple integration,

$$101350 * (\log(28.81) - \log(1.137)) / 1.137 - 101350 * (28.81 - 1.137) = 288124 - 2804658 = -2.516534 * 10^6 \text{ J.}$$

The minus sign indicates an endothermic transition; we need, basically, to put this much work into the system.

This is more energy than simply boiling the water using a heater, and we've not even begun to vaporize the water yet.

I'm not sure how to proceed from here. As the water vaporizes, the pressure rises; the vacuum pump will therefore have to expend more work. The simplest way I can think of to properly calculate this is to assume a constant pressure on both sides of the piston and simply move it 28.81 more meters, for a total work of

$$(4000 - 101350) * (28.81) = -2.805 * 10^6 \text{ J.}$$

Total energy cost using a vacuum pump: $-5.32 * 10^6 \text{ J}$ — more than double that used by a simple heater.

For a 60W vacuum pump, it would take more than a day.

Upon rereading your diatribe, you stated a gallon. Quadruple everything. :-)

However, I should note that the pump cheats. Take a cube of hot water at 373 K, rather than 300K. The vapor pressure of hot water is greater than cold water (indeed, at 100C = 373K the pressure is 1 atm or 101350 Pascal), and the work done by the vacuum pump is far less — until the water cools to 300 K, of course, but there's less water by then.

However, there's no way around that vaporization J/kg figure.

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It's still legal to go .sigless.