

Re: A simple but confusing question

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Here I am trying to clarify some trifling misunderstandings (imho) in Ian's message, news:<ck3b9b\$qr\$1@news-sop.inria.fr> (7 Oct 2004 14:02:49 +0200). I postpone discussing some very interesting issues raised by him (in another message) and other posters.

>One must take a bit of care in comparing these examples. The >coin tossing experiment corresponds to sampling with replacement.

It is the other way around, as I reckon this matter. Lewis Carroll does not assume that the bucket initially had half of its balls white; he assumes that someone has stuffed that bucket choosing the color of each ball by tossing a fair coin. Therefore, each time we pick blindly a ball (without replacement) and then record its color, we just record the outcome of the related coin toss. The remaining balls in the bucket might as well have been in a different bucket; we learn nothing about them.

On the other hand, if we replace this ball in the bucket -- say its color was white -- then the next drawing comes from a different population: of the N balls, we know that $N-1$ of them have $\Pr(w)=0.5$, plus one ball having $\Pr(w)=1.0$. Therefore the new prior for p is again a delta function but is set, instead of 0.5, at $(0.5(N-1) + 1.0)/N$.

That is why the coin-tossing example corresponds to sampling Carroll's bucket *without* replacement. I repeat, our absolute certainty refers not to half of the balls being white, but to the fairness of the coin of the woman who has prepared the bucket.

>We discard the assumption $p = 1/2$ when the data overwhelm our prior >information. How is this a paradox? In practice, we never have delta >function prior knowledge, since this requires infinite precision >measurements.

We do not disagree here!

That is why I call this example a 'paradox'. This not to say that

the method is suspicious, as the term 'paradox' is understood often (e.g., Stone's paradoxes, marginalization "paradox"...).

I only meant that, if one insists that the coin was fair, inspite of sampling 100 white balls and no black ball, her/his attitude would be called "audacity" at best.

>From the American Heritage Dictionary, 3rd Ed., e-version, cop. 1992

~~~~ paradox ~~~~

1. A seemingly contradictory statement that may nonetheless be true.
2. One exhibiting inexplicable or contradictory aspects.
3. An assertion that is essentially self-contradictory, though based on a valid deduction from acceptable premises.
4. A statement contrary to received opinion.

I had in mind meaning [1], and perhaps also [4], if by 'received' we understand 'naive but entrenched'.

(Greek "doxa" is an opinion relative to the thinker or his cohort, rather than an objectively justified conclusion.)

The illustrious paradoxes in statistics correspond to meaning [2]. Sometimes the paradox is a full-blown contradiction, but people want to speak softly about it. Then the real paradox imo is that people want to play down a contradiction and try to "live" with it. (That is, it does not fit my naive and entrenched opinions about how people should act.)

~ George Kahrmanis