

Re: random numbers from a lognormal distribution

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On Tue, 01 Feb 2005 20:33:15 -0600, Ray Koopman wrote:

> *Bob Wheeler wrote:*

>> [...]

>> *I think he is asking how to do it himself. If X is a standard normal variate, then $U=(\log(X)-m)/s$ is lognormal with mean $\exp(m)\sqrt{w}$, where $w=\exp(s^2)$, and variance $\exp(2m)w(w-1)$.*

>

> *Shouldn't that be "If X is a standard normal variate then $U=\exp(X*s+m)$ is lognormal ..."?*

This confusion reminds me of a trick I figured out for working with the lognormal distribution...

I always had trouble working with the formulas for converting the mean and standard deviation from the normal distribution to the lognormal distribution, and vice versa, $E(x) \rightarrow E(\ln x)$, $V(x) \rightarrow V(\ln x)$ and so forth. One day it occurred to me that both distributions are completely characterized by 2 pieces of information, and that the mean and standard deviation aren't the only 2 pieces of information I could use. They're the traditional pieces of information, but they're not the only ones.

I discovered that the median and interquartile range are much easier to use, so that's what I use now.

The transformation functions $\exp(x)$ and $\ln(x)$ are non-decreasing functions, and for any non-decreasing function $g(x)$, the percentiles of x and $g(x)$ are easy to derive from each other. If x_p is the p -th percentile of the random variable x , then $g(x_p)$ is the p -th percentile of the random variable $g(x)$.

In particular, if m is the median of a normal distribution, then $\ln(m)$ is the median of the corresponding lognormal distribution. And if m is the median of a lognormal distribution, then $\exp(m)$ is the median of the corresponding normal distribution. The same goes for the 25-th and 75-th percentiles, and that allows me to calculate the interquartile ranges of both distributions fairly easily.

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So now whenever I work with the lognormal distribution, I use the median and interquartile range as my 2 pieces of information instead of the mean and standard deviation. Try it. I like it much better.