

Re: Bayesian estimation of structured correlation/covariance

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- *From:* "Ben Lee" <benjamin.n.lee@xxxxxxxxx>
 - *Date:* 28 Nov 2005 12:03:00 -0800
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Thanks for the detailed reply,

I will definitely look into Gibbs Sampling more. The other alternative I was considering was just making Naive assumptions about conditional independence – for instance, I have the framework for estimating the unknown correlation variables given an observed correlation between a pair of paths. Empirically, it seems the estimation results are pretty good if I assume that I can simply multiply the likelihoods from different pairs of paths to obtain the overall likelihood.

Ben Lee

David Jones wrote:

> Ben Lee wrote:

>>> Of course, I can measure several paths, so from what I've read, I

>> should formulate this as covariance matrix estimation with the

> Wishart

>> distribution.

>>

>> I'd prefer correlation estimation which I understand from a

> bivariate

>> angle with the Fisher transform – but from what I've read from

>> discussion in this group, the multivariate case gets quite nasty.

>>

>

> For your situation you might need to avoid something which make the

> large step of using the Wishart/ inverse Wishart distribution for the

> covariance matrix. This is because of the structured nature of the

> correlation/covariance you want to impose. An alternative is to become

> invested (more fully invested) in the modern computational approaches

> to Bayesian statistics based on MCMC (Monte Carlo Markov Chains).

>

> For example, in one approach based on "Gibbs sampling" you can arrive

> a situation where your computations for the covariance matrix are

> converted to a case where the elements of the sample covariance matrix

> can be treated as regression coefficients in a simplified problem that

> allows their joint distribution to be described as multivariate

> Normal. (The simplified problem arises because certain of the model

> parameters are being temporarily treated as known). Your constraints

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- > are then converted into information about the mean values for certain
- > of the marginal distributions or for certain linear combinations of
- > the marginal variables (the regression coefficients). The known
- > information is then implemented in the computations essentially by
- > using the theory for going from a joint multivariate Normal
- > distribution for (X,Y) to the conditional distribution (X|Y), where
- > here for example Y might be the set of sample regression coefficients
- > for pairs of variables where the true covariance (and regression
- > coefficient) is known to be zero. This works for the "known zero
- > correlation case" and possibly for the "known equal correlation case",
- > but you would need to look into the theory in more detail.
- >
- > The above is very much a from-first-principles approach that would
- > need substantial effort to work out in detail. You may find that
- > literature already exists for the general problem of structured
- > correlation matrices, particularly for cases where some correlations
- > are assumed to be zero.
- >
- > If you don't find an MCMC approach appealing you may still be best to
- > switch from viewing your problem as one of estimating the covariance
- > matrix, to one where you are estimating a set of regression
- > relationships.
- >
- > David Jones

• **References:**

- ◆ **[Bayesian estimation of structured correlation/covariance](#)**
◇ From: Ben Lee
- ◆ **[Re: Bayesian estimation of structured correlation/covariance](#)**
◇ From: David Jones

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