

## Re: Simple question on Shannon's 1948 paper

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Michael wrote:

I am interested in the second unnumbered equation in Part 1 of the paper:

$$N(t) = N(t-t_1) + N(t-t_2) + \dots + N(t-t_n)$$

How do I see that the above equation does what it says it does, and what are the conditions on  $N(t)$ ?

A couple lines before and after define terms. I'll paraphrase:

We are interested in sequences of the symbols  $S_1, \dots, S_n$ . Each symbol  $S_i$  takes  $t_i$  time to transmit.

$N(t)$  = number of sequences of duration  $t$   
= number of sequences of duration  $t$  that end in  $S_1$  + number of sequences of duration  $t$  that end in  $S_2$  + . . . + number of sequences of duration  $t$  that end in  $S_n$   
= number of sequences of duration  $t - t_1 * 1$  + number of sequences of duration  $t - t_2 * 1$  + . . . + number of sequences of duration  $t - t_n * 1$   
=  $N(t-t_1) + N(t-t_2) + \dots + N(t-t_n)$

The third step is the doozy. Basically, we want to show that, for all  $i$   
number of sequences of duration  $t$  that end in  $S_i$  = number of sequences of duration  $t - t_i * 1$

Well, basically, we could write out all the sequences:

SS...SS $i$

where  $S$  is some symbol (any symbol), and the last symbol is  $S_i$ . There could be a bunch of these:

S $1S_i$

S $2S_i$

S $1S_2S_3S_4S_i$

whatever.

Re: Simple question on Shannon's 1948 paper

The total number is (# of sequences  $SS\dots S$ ) \* 1, i.e., the last element of the sequence is fixed as  $S_i$ .

$S_i$  takes  $t_i$  time. Let's suppose we can transmit  $SS\dots S$  in  $t-t_i$  time. Then we can transmit  $SS\dots SS_i$  in  $(t-t_i) + t_i = t$  time. In fact, that's if and only if (details left for you).

Thanks Michael.

You have made it beautifully clear.

I have (if you don't mind) one last question.

I assume  $N(t-t_i) = 0$  if  $t-t_i < 0$ .

My question is what to assume about  $N(0)$ . If  $t_1$  is the smallest of the  $t_i$ 's and I choose  $t=t_1$  then I would expect that  $N(t_1)=1$ .

Plugging this into the formula Shannon derived, I get  $N(t_1)=N(0) + 0 + 0 + \dots$

So I evidently need to take  $N(0)=1$ . Is this correct and if so what is its interpretation?

Thanks again.

Inf.

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